## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## M.A. DEGREE EXAMINATION - ECONOMICS <br> THIRD SEMESTER - APRIL 2010

## ST 3902-STATISTICS FOR ECONOMISTS

Date \& Time: 30/04/2010 / 9:00-12:00
Dept. No. $\square$ Max. : 100 Marks

## SECTION A

## Answer all the questions:

( $10 \times 2=20$ Marks)

1. Write any two properties of arithmetic mean.
2. If the mean and median for an asymmetric distribution are respectively 20 and 25 find an approximate value of mode.
3. Provide axiomatic definition of probability.
4. Define binomial distribution.
5. What are the probabilities of Type I and Type II errors?
6. Write any two applications of $t$ distribution.
7. What is a time series ?
8. Define an index number.
9. Define basic solution to a given system of linear equations.
10. Express transportation problem as an LPP.

## SECTION B

Answer any five questions:
11. Calculate mode using the empirical formula for the following data:
$\begin{array}{lllllll}\text { Marks } & : 0-10 & 10-20 & 20-30 & 30-40 & 40-50 & 50-60\end{array}$
$\begin{array}{lllllll}\text { No.of students: } & 6 & 12 & 20 & 35 & 18 & 4\end{array}$
12. Find the Karl Pearson's coefficient of correlation for the following data:

X:43 $44 \quad 46 \quad 40 \quad 44 \quad 42 \quad 45 \quad 42 \quad 38 \quad 40 \quad 42 \quad 57$
$\mathrm{Y}: 29 \quad 31 \quad 19 \quad 18 \quad 19 \quad 27 \quad 27 \quad 29 \quad 41 \quad 30 \quad 26 \quad 10$
13. Ten fair coins were thrown simultaneously. Find the probability of getting (i) at least one head (ii) exactly five heads (iii) at most seven heads (iv) not more than four heads.
14. A random sample of 200 tins of coconut oil gave an average weight of 4.95 kgs with a standard of 0.21 kg . Do we accept the hypothesis of net weight 5 kgs per tin at $1 \%$ level?
15. If $X$ has the probability density function

$$
f(x)=6 x(1-x), 0 \leq x \leq 1 ; f(x)=0 \text { otherwise, }
$$

find mean and variance of $X$.
16. In a distribution exactly normal , $10.03 \%$ of the items are under 25 kg weight and $89.97 \%$ of the items are under 70 kg weight. What are mean and standard of the distribution?
17. Explain the components of time series.
18. Use graphical method to

Maximize $\mathrm{z}=50 \mathrm{x}_{1}+60 \mathrm{x}_{2}$
subject to
$2 \mathrm{x}_{1}+3 \mathrm{x}_{2} \leq 1500 ; 3 \mathrm{x}_{1}+2 \mathrm{x}_{2} \leq 1500 ; 0 \leq \mathrm{x}_{1} \leq 400 ; 0 \leq \mathrm{x}_{2} \leq 400$.

## SECTION C

## Answer any two questions:

19. A factory produces two types of electric bulbs A and B. In an experiment relating to their life, the following results were obtained.
Length of life(in hrs) : 500-700 700-900 $\quad 900-1100 \quad 1100-1300 \quad 1300-1500$
$\begin{array}{lllllll}\text { No.of bulbs(A) } & : & 5 & 11 & 26 & 10 & 8\end{array}$
$\begin{array}{lllllll}\text { No.of bulbs(B) } & : & 4 & 30 & 12 & 8 & 6\end{array}$
Compare the variability of the two varieties using the coefficient of variation.
20. Seven fair coins were tossed and the number of heads noted. The experiment was repeated 128 times and the following distribution was obtained.

Frequency : $7 \quad \begin{array}{llllllll}7 & 6 & 19 & 35 & 30 & 23 & 7 & 1\end{array}$
Fit a binomial distribution assuming (i) the coin is unbiased (ii) the nature of the coin is not known. Also test the goodness of fit at $5 \%$ level.
21. Calculate seasonal indices by the ratio-to moving average method from the following method:

|  | Year |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Quarter | 1980 | 1981 | 1982 | 1983 |
| $\mathrm{Q}_{1}$ | 75 | 86 | 90 | 100 |
| $\mathrm{Q}_{2}$ | 60 | 65 | 72 | 78 |
| $\mathrm{Q}_{3}$ | 54 | 63 | 66 | 72 |
| $\mathrm{Q}_{4}$ | 59 | 80 | 85 | 93 |

22. Find the optimal solution to the following transportation problem:

Destination

| Origin | $D_{1}$ | $D_{2}$ | $D_{3}$ | $D_{4}$ | Supply |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{O}_{1}$ | 23 | 27 | 16 | 18 | 30 |
| $\mathrm{O}_{2}$ | 12 | 17 | 20 | 51 | 40 |
| $\mathrm{O}_{3}$ | 22 | 28 | 12 | 32 | 53 |
| Demand | 22 | 35 | 25 | 41 |  |

